

Dear student following is an easy level [ ● ○ ○ ] test paper. Score of 24 Marks in 15 Minutes would be a satisfactory performance. Questions 1-10(+3, -1) (All questions have only one option correct)

- Q.1** If the coefficients of 2nd, 3rd and 4th terms in the expansion of  $(1 + x)^n$  are in A.P. then n equals  
 (A) 2 (B) 7  
 (C) 9 (D) None of these
- Q.2** The coefficient of  $x^{10}$  in the expansion  $(1 + x^2 - x^3)^8$  is  
 (A) 476 (B) 496  
 (C) 506 (D) 528
- Q.3** The value of expression  $\frac{{}^{10}C_r}{{}^{11}C_r}$  when both numerator and denominator have their greatest value is  
 (A)  $\frac{10}{11}$  (B)  $\frac{6}{5}$   
 (C)  $\frac{6}{11}$  (D) None of these
- Q.4** The coefficient of  $x^4$  in the expansion of  $(1 + x + x^2 + x^3)^n$  is  
 (A)  ${}^nC_1 \times {}^nC_2 + {}^nC_2 + {}^nC_4$   
 (B)  ${}^nC_1 \times {}^nC_3 + {}^nC_2 + {}^nC_4$   
 (C)  ${}^nC_2 \times {}^nC_2 + {}^nC_4$  (D) None of these
- Q.5** If the coefficient of  $x^7$  and  $x^8$  in  $\left(2 + \frac{x}{3}\right)^n$  are equal, then value of n is  
 (A) 56 (B) 55  
 (C) 47 (D) 19
- Q.6** If A and B are coefficients of  $x^n$  in the expansions of  $(1 + x)^{2n}$  and  $(1 + x)^{2n-1}$  respectively, then  
 (A)  $A = B$  (B)  $A = 2B$   
 (C)  $2A = B$  (D) None of these
- Q.7** In the expansion of  $(1 + px)^n$ ,  $n \in \mathbb{N}$ , the coefficient of x and  $x^2$  are 8 and 24 respectively, then  
 (A)  $n = 3, p = 2$  (B)  $n = 4, p = 2$   
 (C)  $n = 4, p = 3$  (D)  $n = 5, p = 3$
- Q.8** The term independent of x in the expansion of  $\left(2x + \frac{1}{3x^2}\right)^9$  is  
 (A) 2<sup>nd</sup> (B) 3<sup>rd</sup> (C) 4<sup>th</sup> (D) 5<sup>th</sup>
- Q.9** The middle term in the expansion of  $\left(\frac{2}{3}x - \frac{3}{2}y\right)^{20}$  is  
 (A)  ${}^{20}C_{10} x^{10} y^{10}$  (B)  $x^{10} y^{10}$   
 (C)  ${}^{20}C_{10} (2/3)^{10} (xy)^{10}$  (D)  $-x^{10} y^{10}$
- Q.10** Coefficient of  $x^4$  in the expansion of  $\frac{1 - 3x + x^2}{e^x}$  is  
 (A)  $\frac{25}{24}$  (B)  $n \frac{24}{25}$   
 (C)  $\frac{4}{25}$  (D)  $\frac{25}{4}$

MATHEMATICS IIT JEE ( SEPT.4<sup>th</sup> WEEK CLASS TEST 1) (BINOMIAL THEOREM) ANSWER KEY

Name : ..... Roll No. : .....

	A	B	C	D		A	B	C	D		A	B	C	D
1	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	4	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	7	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
2	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	5	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	8	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
3	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	6	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	9	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
										10	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>

**ANSWER KEY**

Que.	1	2	3	4	5	6	7	8	9	10
Ans.	B	A	C	A	B	B	B	C	A	A

**SOLUTIONS**
**Sol.1 (B)**

The coefficients of 2nd term is  ${}^n C_1$

The coefficients of 3rd term in =  ${}^n C_2$

The coefficients of 4th term is =  ${}^n C_3$

∴ These coefficients are in A.P

$$\therefore 2 \cdot {}^n C_2 = {}^n C_1 + {}^n C_3$$

$$2 \cdot \frac{n(n-1)}{2!} = n + \frac{n(n-1)(n-2)}{3!}$$

$$\Rightarrow 6(n-1) = 6 + (n^2 - 3n + 2)$$

$$[\because n \neq 0]$$

$$\Rightarrow n^2 - 9n + 14 = 0 \Rightarrow n = 2, 7$$

But  $n = 2$  not admissible as expansion contain more than 3 terms.

Thus  $n = 7$

**Sol.2 (A)**

General term in the expansion of  $(1 + x^2 - x^3)^8$  is

$$T = \frac{8!}{p!q!r!} 1^p (x^2)^q (-x^3)^r$$

where  $p + q + r = 8$

$$\text{or } T = \frac{8!}{p!q!r!} (-1)^r x^{2q+3r}$$

$$0 \leq p, q, r \leq 8, p + q + r = 8$$

This will contain  $x^{10}$  if  $2q + 3r = 10$

We can choose,  $p, q, r$  to satisfy all these conditions as follows

$$q = 2, r = 2 \text{ and } p = 4 \text{ and } q = 5, r = 0 \text{ and } p = 3$$

Then coeff. of  $x^{10}$  will be  $\frac{8!}{4!2!2!} (-1)^2$

$$\text{and } \frac{8!}{3!5!0!} (-1)^0$$

Sum of the coeff. of  $x^{10}$  is

$$S = \frac{8!}{4!2!2!} + \frac{8!}{3!5!} = 420 + 56 = 476$$

**Sol.3 (C)**

The greatest value of  ${}^m C_r$  occurs for  $r = m/2$

If  $m$  is even and for  $r = \frac{m-1}{2}$  and

$\frac{m+1}{2}$  when  $m$  is odd.

Thus greatest value of  ${}^{10} C_r = {}^{10} C_5$

and greatest value of  ${}^{11} C_r = {}^{11} C_5, \left[ r = \frac{11-1}{2} \right]$

$$\text{Required value is } \frac{{}^{10} C_5}{{}^{11} C_5} = \frac{10! / 5!5!}{11! / 5!6!} = \frac{6}{11}$$

**Sol.4 (A)**

We have  $(1 + x + x^2 + x^3)^n$

$$= [(1 + x)(1 + x^2)]^n$$

$$= [1 + {}^n C_1 x + {}^n C_2 x^2 + {}^n C_3 x^3 + {}^n C_4 x^4 \dots]$$

$$[1 + {}^n C_1 x^2 + {}^n C_2 x^4 + \dots]$$

Coeff. of  $x^4$  is  $1 \cdot {}^n C_2 + {}^n C_2 \cdot {}^n C_1 + {}^n C_4$

**Sol.5 (B)**

$(r + 1)$ th term in the expansion of  $\left(2 + \frac{x}{3}\right)^n$

is given by

$$T_{r+1} = {}^n C_r 2^{n-r} \left(\frac{x}{3}\right)^r = {}^n C_r \left(\frac{2^{n-r}}{3^r}\right) x^r$$

According to the given condition

$${}^n C_7 \left(\frac{2^{n-7}}{3^7}\right) = {}^n C_8 \left(\frac{2^{n-8}}{3^8}\right)$$

$$\begin{aligned} \Rightarrow \frac{{}^n C_7}{{}^n C_8} &= \frac{2^{n-8}}{3^8} \cdot \frac{3^7}{2^{n-7}} \\ \Rightarrow \frac{n!}{7!(n-7)!} \cdot \frac{8!(n-8)!}{n!} &= \frac{1}{6} \\ \Rightarrow \frac{8}{n-7} &= \frac{1}{6} \\ \Rightarrow 48 &= n-7 \quad \Rightarrow n = 55 \end{aligned}$$

**Sol.6 (B)**

We know that coefficient of  $x^r$  in the expansion of  $(1+x)^m$  is  ${}^m C_r$ .

Thus,  $A = {}^{2n} C_n$  and  $B = {}^{2n-1} C_n$

$$\begin{aligned} \text{We have } \frac{A}{B} &= \frac{{}^{2n} C_n}{{}^{2n-1} C_n} = \frac{(2n)!}{n!n!} \cdot \frac{(n-1)!}{(2n-1)!} \\ &= \frac{2n}{n} = 2 \end{aligned}$$

$$\Rightarrow A = 2B$$

**Sol.7 (B)**

We have

$$\begin{aligned} (1+px)^n &= 1 + {}^n C_1 (px) + {}^n C_2 (px)^2 + \dots \\ &= 1 + np x + \frac{1}{2} n(n-1) p^2 x^2 + \dots \end{aligned}$$

According to the hypothesis,

$$np = 8 \text{ and } \frac{1}{2} n(n-1) p^2 = 24$$

Putting  $P = 8/n$  in the second expression, we get

$$\frac{1}{2} n(n-1) \left(\frac{8}{n}\right)^2 = 24$$

$$\Rightarrow \frac{n-1}{n} = \frac{24 \times 2}{8 \times 8} = \frac{3}{4}$$

$$\Rightarrow 4n - 4 = 3n \quad \Rightarrow n = 4$$

Putting this value in  $np = 8$ , we get  $p = 2$ .

**Sol.8 (C)**

Suppose  $(r+1)$ th term is independent of  $x$ . We have

$$T_{r+1} = {}^9 C_r (2x)^{9-r} \left(\frac{1}{3x^2}\right)^r = {}^9 C_r 2^{9-r} \frac{1}{3^r} \cdot x^{9-3r}$$

This term is independent of  $x$  if  $9-3r = 0$  i.e.,  $r = 3$ .

Thus, 4th term is independent of  $x$ .

**Sol.9 (A)**

The binomial expansion of  $\left(\frac{2}{3}x - \frac{3}{2}y\right)^{20}$

consists of 21 terms. Therefore  $\left(\frac{20}{2} + 1\right)$ th

term, i.e., 11th term is the middle term.

Hence the middle term =  $T_{11} = {}^{20} C_{10}$

$$\left(\frac{2}{3}x\right)^{20-10} \left(-\frac{3}{2}y\right)^{10} = {}^{20} C_{10} x^{10} y^{10}$$

**Sol.10 (A)**

$$\frac{1-3x+x^2}{e^x} = (1-3x+x^2)e^{-x}$$

$$= (1-3x+x^2) \left(1-x+\frac{x^2}{2!}-\frac{x^3}{3!}+\frac{x^4}{4!}-\dots\right)$$

$$\therefore \text{Coefficient of } x^4 = \frac{1}{4!} + \frac{3}{3!} + \frac{1}{2!}$$

$$= \frac{1}{24} + \frac{1}{2} + \frac{1}{2} = \frac{25}{24}$$